

## Data Encoding

- Digital signaling
  - Data source  $g(t)$  encoded into digital signal  $x(t)$ 
    - \*  $g(t)$  itself may be analog or digital
    - \* Actual form of  $x(t)$  dependent on encoding technique, chosen to optimize use of transmission medium
      - conserve bandwidth or minimize errors
- Analog signaling
  - Based on a continuous constant-frequency signal, called the *carrier signal*
  - Carrier signal frequency chosen to be compatible with transmission medium
  - Data transmitted by carrier signal modulation
  - Modulation
    - \* Process of encoding source data onto a carrier signal with frequency  $f_c$
    - \* Operation on one or more of three fundamental frequency-domain parameters – amplitude, frequency, and phase
- Input signal  $m(t)$ 
  - Can be analog or digital
  - Also called *modulating signal* or *baseband signal*
  - Modulated signal  $s(t)$  – result of modulating carrier signal
    - \* Also called bandlimited or bandpass signal
  - Location of bandwidth on the spectrum related to carrier frequency  $f_c$
- Different possible combinations
  - Digital data, digital signal
    - \* Simple and inexpensive equipment
  - Analog data, digital signal
    - \* Data needs to be converted to digital form
  - Digital data, analog signal
    - \* Needed to take advantage of existing transmission media that only allows the transmission of analog signal
  - Analog data, analog signal
    - \* Transmitted as baseband signal easily and cheaply
    - \* Modulation to shift the bandwidth of baseband signal to another portion of spectrum
    - \* Multiple signals on different position on the spectrum can share the same transmission medium (frequency-division multiplexing)

## Digital Data, Digital Signals

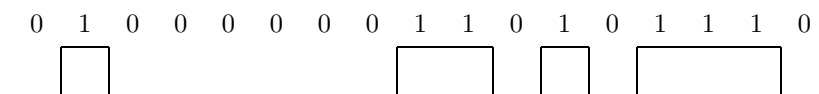
- Digital signal
  - Sequences of discrete, discontinuous voltage pulses
  - Binary data transmitted by encoding each data bit into signal elements

- Unipolar signal
  - All signal elements have the same algebraic sign
  - Binary logic states represented by a positive and negative voltage level
- Data rate
  - Number of bits per second transmitted
  - Duration or length of a bit
    - \* Amount of time required to emit a bit
    - \* For a data rate  $R$  bits per second, duration of each bit is  $\frac{1}{R}$
- Modulation rate
  - Rate at which signal level is changed
  - Depends on the nature of signal encoding
  - Expressed in *bauds*, or signal elements per second
- *Mark* – Binary digit 1
- *Space* – Binary digit 0
- Interpreting digital signal at the receiver
  - Receiver must know the timing of each bit (start and end)
  - Determine if the signal level for bit is high (1) or low (0)
  - Sampling and comparison with a threshold value
  - Important factors: SNR, data rate, and bandwidth
  - Important facts:
    1. Increase in data rate increases bit-error-rate (BER)
    2. Increase in SNR decreases BER
    3. Increase in bandwidth allows for an increase in data rate
- Encoding scheme
  - Mapping from data bits to signal elements
- Evaluation and comparison of various schemes
  - Signal spectrum
    - \* Lack of high frequency components implies less bandwidth requirement
    - \* Lack of DC component is desirable
    - \* DC component requires direct physical attachment between transmission components
    - \* No DC component means that AC coupling via transformer is possible, providing electrical isolation and reducing interference
    - \* Magnitude of the effect of signal distortion and interference depend on the spectral properties of transmitted signal
    - \* Good signal design should concentrate in the middle of transmission bandwidth to avoid band edges
    - \* Code can be designed with the aim of shaping the spectrum of transmitted signal
  - Clocking
    - \* Beginning and end of each bit needs to be synchronized
    - \* Provide synchronization based on transmitted signal
  - Error detection

- \* Part of data link control layer
- \* Useful to build into physical signal encoding scheme
- Signal interference and noise immunity
  - \* Expressed in terms of BER
- Cost and complexity
  - \* Cost is proportional to data rate

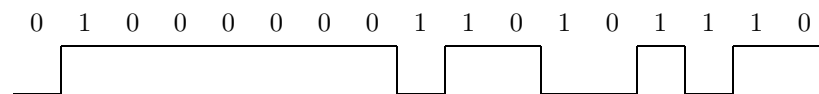
- Nonreturn to zero (NRZ)

- Use two different voltage levels for two binary digits
- Voltage level constant during bit interval
  - \* No transition, no return to zero voltage level
- Nonreturn to zero-level (NRZ-L)
  - \* Negative voltage level represents one bit value while positive voltage level represents the other bit value



- \* Generally the code used to generate or interpret digital data by terminals and other devices
- \* NRZ-L is  $g(t)$  (source signal) while the encoded form is  $x(t)$
- Nonreturn to zero, invert on ones (NRZI)

- \* Variation of NRZ
- \* Maintains a constant voltage pulse for bit duration (same as NRZ-L)
- \* Data encoded as presence or absence of signal transition at bit start time
- \* Transition indicates 1 while no transition indicates 0

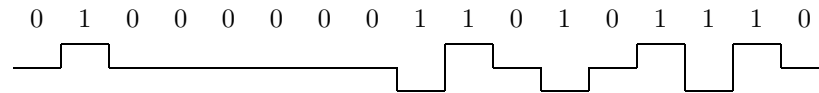


- *Differential encoding*
  - \* Exemplified by NRZI
  - \* Information represented as changes between successive data symbols rather than signal elements
  - \* Encoding of current bit is determined as
    - Current bit 0? Encoded with the same signal as preceding bit
    - Current bit 1? Encoded with different signal as preceding bit
  - \* More reliable to detect transition in the presence of noise than to compare the value to a threshold
  - \* Impervious to reversal of polarity in NRZ-L
- Limitations
  - \* Presence of DC component
  - \* Lack of synchronization capability
  - \* Any drift between timing of transmitter and receiver during a long sequence of 0's or 1's can result in loss of synchronization
- Applications
  - \* Commonly used for digital magnetic recording
  - \* Not attractive for signal transmission applications

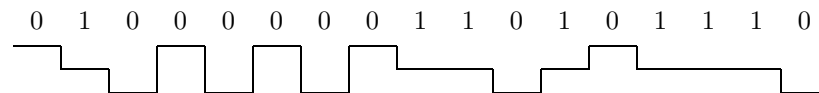
- Multilevel binary

- Addresses some of the deficiencies of NRZ codes

- Use more than two signal levels
- Bipolar-AMI (Automatic Mark Inversion)
  - \* Binary 0 is represented by no line signal
  - \* Binary 1 is represented by positive or negative pulse
  - \* Binary 1 pulses must alternate in polarity



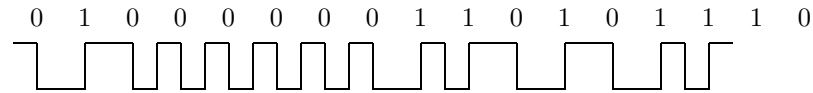
- \* Advantages
  - No loss of synchronization with a long string of 1's
  - Each 1 introduces a transition and receiver can resynchronize on transition
  - Long string of 0's still a problem
  - Because 1 signals alternate in voltage from positive to negative, there is no net DC component
  - Bandwidth of resulting signal considerably less than bandwidth for NRZ
  - Pulse alternation provides a simple means of error detection; any isolated error (addition or deletion of pulse) causes a violation
- Pseudoternary
  - \* Binary 1 represented by absence of line signal
  - \* Binary 0 represented by alternating positive and negative pulses
  - \* Almost opposite representation compared to bipolar-AMI



- Long string of 0's in bipolar-AMI and a long string of 1's in pseudoternary still presents a problem
  - \* May insert additional bits to force transitions
    - Used in ISDN for relatively low data rate transmission
    - Expensive in high data rate because it results in an increase in already high signal transmission rate
    - Possible to apply at high data rate using data scrambling
  - \* Line signal may take one of three levels
    - Each signal element can represent  $\log_2 3 = 1.58$  bits of information but actually represents only one bit
    - Loss of efficiency compared to NRZ
    - Receiver has to discriminate between three levels ( $+A, 0, -A$ )
    - Signal requires approximately 3dB more power than the corresponding 2-valued signal for the same BER
    - BER for NRZ codes is significantly less than multilevel binary for the same SNR

- Biphase

- Overcome the limitations of NRZ codes
- Require at least one transition per bit time and may even have two transitions
- Manchester code
  - \* Transition at the middle of each bit period
  - \* Serves as clocking mechanism as well as data
  - \* Transition from low to high indicates 1 while transition from high to low indicates 0



– Differential Manchester

- \* Midbit transition is used only to provide clocking
- \* 0 is represented by presence of transition at the beginning of bit period
- \* 1 is represented by the absence of transition at the beginning of bit period
- \* Advantage of employing differential encoding (no DC)

0

– Maximum modulation rate is twice that for NRZ due to one transition per bit time

- \* Bandwidth required is correspondingly greater

– Advantages

- \* Synchronization
  - Predictable transition during each bit time
  - Can be used for synchronization
  - *Self-clocking codes*
- \* No DC component
- \* Error detection
  - Can be detected by absence of expected transition
  - Impervious to noise as noise will have to invert the signal both before and after the expected transition

– Bandwidth reasonably narrow with no DC component

- \* Bandwidth wider than that for multilevel binary codes

– Popular for data transmission

- \* Manchester used for baseband coaxial cable and twisted pair bus LANs
- \* Differential Manchester used for token ring LAN using shielded twisted pair

• Modulation rate

– Data rate

- \* Bits per second, or bit rate
- \*  $\frac{1}{t_B}$  where  $t_B$  is bit duration

– Modulation rate

- \* Baud
- \* Rate at which signal elements are generated

– Manchester code

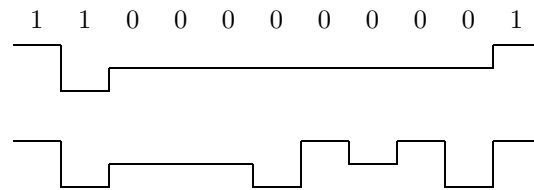
- \* Minimum size signal element is a pulse of one-half the duration of bit interval
- \* All 0's or all 1's generate a continuous stream of such pulses
- \* Maximum modulation rate is  $\frac{2}{t_B}$

– Modulation rate  $D = \frac{R}{b}$  where  $R$  is the data rate in bps and  $b$  is the number of bits per signal element

• Scrambling techniques

- Biphase techniques require high signal rate relative to data rate limiting their use in long distance applications

- Scrambling can remove the above limitation
- Constant voltage level sequences are replaced by fillers to provide synchronization for receiver clock
- Filler must be recognized by receiver and replaced by original data sequence
- Filler sequence is the same length as original sequence, implying no increase in data rate
- Design goals
  - \* No DC component
  - \* No long sequences of zero-level line signals
  - \* No reduction in data rate
  - \* Error-detection capability
- Bipolar with 8-zeros substitution (B8ZS)
  - \* Commonly used in North America
  - \* Based on bipolar-AMI
  - \* Encoding amended with following rules
    - If there is an octet of all zeros, and last voltage preceding this octet was positive, then the octet is encoded as 000 + −0 − +.
    - If there is an octet of all zeros, and last voltage preceding this octet was negative, then the octet is encoded as 000 − +0 + −.
  - \* Forces two code violations of the AMI code, using patterns not allowed in AMI
    - Receiver recognizes the pattern and interprets the octet as all zeros



- High-density bipolar-3 zeros (HDB3)
    - \* Commonly used in Europe and Japan
    - \* Based on bipolar-AMI
    - \* Replaces strings of four zeros with one or two pulses
      - In each case, fourth zero is replaced with a code violation
    - \* A rule is added to ensure that successive violations are of alternate polarity to avoid DC component
- | Polarity of preceding pulse | Number of bipolar pulses (ones) since last substitution |      |
|-----------------------------|---|------|
|                             | Odd   | Even |
| −                           | 000−  | +00+ |
| +                           | 000+  | −00− |
- \* If last violation was positive, this violation must be negative, and vice versa

## Digital data, analog signals

- Transmission of digital data through public phone network
  - Phone network works with voice frequency range of 300 to 3400 Hz
  - Not currently suitable for handling digital signals from subscriber location
  - Digital devices attached to network via modems, to produce signals in voice frequency range
- Encoding techniques

- Based on modifying one of the three characteristics of carrier signal: amplitude, frequency, and phase, as described below

- \* In each case, resulting signal occupies a bandwidth centered on carrier frequency

- Amplitude-shift keying (ASK)

- \* Two binary values are represented by two different amplitudes of carrier signal

- \* One of the amplitudes is zero

- One binary digit is represented by the presence of the carrier, the other by the absence of the carrier

- \* Resulting signal is

$$s(t) = \begin{cases} A \cos(2\pi f_c t) & \text{binary 1} \\ 0 & \text{binary 0} \end{cases}$$

where the carrier signal is given by  $A \cos(2\pi f_c t)$

- \* Susceptible to sudden gain changes

- \* Typically used only up to 1200 bps on voice grade lines

- \* Used to transmit digital data over optical fiber

- For LED transmitters, presence of light pulse indicates a 1 while the absence of light pulse indicates a zero
    - For laser transmitters, a low light level indicates one signal element while a high amplitude light-wave represents the other signal element

- Frequency-shift keying (FSK)

- \* Two binary values are represented by two different frequencies near the carrier frequency

- \* Resulting signal is

$$s(t) = \begin{cases} A \cos(2\pi f_1 t) & \text{binary 1} \\ A \cos(2\pi f_2 t) & \text{binary 0} \end{cases}$$

where  $f_1$  and  $f_2$  are offset from carrier frequency  $f_c$  by equal but opposite amounts

- \* Full duplex transmission over voice grade line

- Voice grade line passes frequencies between 300 to 3400 Hz
    - In one direction,  $f_c$  is 1170 Hz with  $f_1$  and  $f_2$  given by  $\pm 100$  Hz
    - In other direction,  $f_c$  is 2125 Hz  $\pm 100$  Hz
    - There is little overlap and hence, little interference

- \* Less susceptible to error compared to ASK

- \* Used up to 1200 bps on voice grade lines

- \* Also used for high frequency (3 to 30 MHz) radio transmission

- \* Can be used at even higher frequencies in LANs on coaxial cables

- Phase-shift keying (PSK)

- \* Data is represented by carrier signal phase-shift to indicate different values

- \* Two-phase system with differential PSK

- Phase shift is with respect to the previous bit transmitted rather than some constant reference signal
    - Binary zero is represented by sending a signal burst of the same phase as the previous signal burst
    - Binary one is represented by sending a signal burst of the opposite phase as the previous signal burst
    - Resulting signal is

$$s(t) = \begin{cases} A \cos(2\pi f_c t + \pi) & \text{binary 1} \\ A \cos(2\pi f_c t) & \text{binary 0} \end{cases}$$

with the phase measured relative to previous bit interval

- \* Bandwidth can be used more effectively by representing more than one bit in each signal element

- Instead of a phase shift of  $180^\circ$  as in differential PSK, quadratic PSK, or QPSK uses phase shifts of multiples of  $90^\circ$
- Resulting signal is

$$s(t) = \begin{cases} A \cos(2\pi f_c t + \frac{\pi}{4}) & 11 \\ A \cos(2\pi f_c t + \frac{3\pi}{4}) & 10 \\ A \cos(2\pi f_c t + \frac{5\pi}{4}) & 00 \\ A \cos(2\pi f_c t + \frac{7\pi}{4}) & 01 \end{cases}$$

- Each signal element represents 2 bits instead of 1
- Can be extended to transmit three bits at a time using eight different phase angles
- Each phase angle can have more than one amplitude
- A standard 9600 bps modem uses 12 phase angles, four of which have two amplitude values
- \* Difference between  $R$  (data rate in bps) and  $D$  (modulation rate in bauds)
  - Assume the scheme being used with NRZ-L digital input
  - Data rate  $R = \frac{1}{t_B}$  where  $t_B$  is width of each NRZ-L bit
  - Encoded signal contains 4 bits in each signal element using  $L = 16$  different combinations of amplitude and phase
  - Modulation rate  $D = \frac{R}{4}$ , because each change of signal element communicates four bits
  - Line signaling speed is 2400 baud but data rate is 9600 bps, allowing higher bit rates on voice grade lines using complex modulation schemes

\* In general

$$D = \frac{R}{b} = \frac{R}{\log_2 L}$$

where

$D$	modulation rate in baud
$R$	data rate in bps
$L$	number of different signal elements
$b$	number of bits per signal element

#### • Performance

- Bandwidth of modulated signal depends on factors such as
  - \* Definition of bandwidth used
  - \* Filtering technique used to create bandpass signal
- Transmission bandwidth  $B_T$  for ASK and PSK is of the form

$$B_T = (1 + r)R$$

where  $R$  is the bit rate and  $r$  is related to the technique by which the signal is filtered to establish bandwidth for transmission; typically  $0 < r < 1$

$$* B_T \propto R$$

- For FSK, we have

$$B_T = 2\Delta F + (1 + r)R$$

where  $\Delta F = f_2 - f_c = f_c - f_1$

- \* For high frequencies,  $\Delta F$  term dominates
- \* FSK signaling on coaxial cable multipoint local network uses  $\Delta F = 1.25$  MHz,  $f_c = 5$  MHz, and  $R = 1$  Mbps, giving  $2\Delta F = 2.5$  MHz as the dominant term
- \* For low frequency (voice grade line modem), we have  $\Delta F = 100$  Hz,  $f_c = 1170$  Hz in one direction, and  $R = 300$  bps, so that the  $(1 + r)R$  term dominates



- With multilevel signaling, bandwidth can improve significantly

$$B_T = \left( \frac{1+r}{b} \right) R = \left( \frac{1+r}{\log_2 L} \right) R$$

- Relationship with bandwidth efficiency

- \* We have

$$\frac{E_b}{N_0} = \frac{S}{N_0 R}$$

where  $N_0$  is the noise power density in watts/Hz

- \* Noise in a signal with bandwidth  $B_T$  is given by

$$N = N_0 B_T$$

- \* Substituting for  $N_0$ , we have

$$\frac{E_b}{N_0} = \frac{S}{N} \cdot \frac{B_T}{R}$$

- \* Thus, bit error rate can be reduced by increasing bandwidth efficiency  $\frac{E_b}{N_0}$ , or by
  - Increasing the bandwidth, or
  - Decreasing the data rate

- Example: Bandwidth efficiency for FSK, ASK, PSK, and QPSK for a bit error rate of  $10^{-7}$  on a channel with an SNR of 12 dB

- \* Efficiency is given by

$$\frac{E_b}{N_0} = 12 \text{ dB} - \left( \frac{R}{B_T} \right)_{\text{dB}}$$

- \* For FSK and ASK, we get from Figure 5.4 (p. 138)

$$\frac{E_b}{N_0} = 14.2 \text{ dB}$$

which yields

$$\left( \frac{R}{B_T} \right)_{\text{dB}} = -2.2 \text{ dB}$$

- \* For PSK, we get from Figure 5.4 (p. 138)

$$\frac{E_b}{N_0} = 11.2 \text{ dB}$$

which yields

$$\left( \frac{R}{B_T} \right)_{\text{dB}} = 0.8 \text{ dB}$$

- \* For QPSK, baud rate  $D = \frac{R}{2}$  so that

$$\frac{R}{B_T} = 1.6 \text{ dB}$$

## Analog data, digital signals

- Digitization: Converting analog data into digital signals
- After digitization, one of the following can happen

1. Figure 5.9

2. Digital data can be transmitted using NRZ-L, going directly from analog to digital signal
3. Digital data can be encoded as a digital signal using a code other than NRZ-L
4. Digital data can be converted into analog signal, using one of the modulation techniques
  - Allows analog data to be treated as digital data, even though it is transmitted as analog data

- Codec

- Device used to convert analog data into digital form for transmission and subsequently, recover the analog data from digital signal
- Uses pulse code modulation or delta modulation

- Pulse code modulation (PCM)

- Based on sampling theorem

If a signal  $f(t)$  is sampled at regular intervals of time and at a rate higher than twice the highest signal frequency, then the samples contain all the information of the original signal. The function  $f(t)$  may be reconstructed from these samples by the use of a low-pass filter.

- Limiting voice signals to 4000 Hz allows us to characterize them completely by 8000 samples per second
  - \* Analog samples, or pulse amplitude modulated (PAM) samples
  - \* Each analog sample is assigned a binary code to convert to digital
  - \* 8-bit per sample, gives  $8000 \times 8 = 64\text{kbps}$  for each voice channel
  - \* Figure 5.10
- PCM starts with a continuous-time, continuous-amplitude (analog) signal
  - \* Analog signal is converted to digital
    - Blocks of  $n$  bits, with each  $n$ -bit number representing the amplitude of a PCM pulse
  - \* On reception, digital signal is converted back to analog
    - Violates the sampling theorem
    - Quantization of PAM pulse only allows the original signal to be approximated and not recovered exactly, leading to *quantizing error* or *quantizing noise*
    - Signal-to-noise ratio for the quantizing noise can be expressed as

$$\begin{aligned}\text{SNR} &= 20 \log 2^n + 1.76 \text{ dB} \\ &= 6.02n + 1.76 \text{ dB}\end{aligned}$$

- For each additional bit used for quantizing, SNR increases by about 6 dB, or a factor of 4

- Nonlinear encoding

- \* Refinement of PCM
- \* Quantization levels are not equally spaced
- \* Greater number of quantization steps for lower amplitudes and smaller number of steps for higher amplitudes allows for reduction in overall signal distortion
- \* Figure 5.11

- Companding

- \* Compressing-expanding
- \* Achieves similar effect to nonlinear encoding
- \* Compresses intensity range of a signal by imparting more gain to weak signals than to strong signals on input
- \* Reverse operation is performed on output

- Delta modulation (DM)

- Alternative to PCM
- Analog input is approximated by a staircase function that moves up or down one quantization level ( $\delta$ ) at each sampling interval  $T_s$
- Figure 5.13
- A bit stream is produced by approximating the derivative of an analog signal rather than its amplitude
  - \* Produce a 1 if staircase function is to go up during next interval
  - \* Produce a 0 otherwise
- Transition at each sampling interval is chosen so that staircase function tracks the original waveform as closely as possible
  - \* Based on a feedback mechanism
  - \* Figure 5.14
  - \* Analog input is compared to the most recent value of approximating staircase function
    - If value exceeds the staircase function, generate a 1
    - Otherwise generate a 0
  - \* Staircase is always changed in the direction of the input signal
  - \* Output of DM process is a binary sequence to be used for reconstructing the staircase function
    - Reconstructed staircase function is smoothed by lowpass filter to reconstruct analog approximation of analog input signal
- Two important parameters in DM scheme
  1. Sampling rate
  2. Size of step assigned to each binary digit  $\delta$ 
    - \* Must be chosen to produce a balance between two types of errors or noise
    - \* If waveform changes slowly, there is quantizing noise that increases with an increase in  $\delta$
    - \* If analog waveform changes rapidly than the staircase can keep up with, there is slope overhead noise that increases with a decrease in  $\delta$
- Principal advantage of DM is its simplicity of implementation
- PCM has better SNR characteristics at the same data rate
- Performance
  - PCM can produced good noise reproduction with 128 quantization levels or 7-bit coding
  - With a bandwidth of 4 kHz, samples must be taken at a rate of 8000 samples per second (2 samples per cycle), giving a data rate of  $8000 \times 7 = 56$  kbps for PCM-encoded signal
  - Bandwidth requirement
    - \* Digital transmission requires 56 kbps for 4 kHz analog signal
    - \* Using Nyquist criterion, this signal could require on the order of 28 kHz of bandwidth
    - \* Why do digital signals still grow in popularity?
      - No additive noise because of repeaters instead of amplifiers
      - Digital signals use time division multiplexing instead of frequency division multiplexing used for analog signals; no intermodulation noise
      - More efficient digital switching techniques

## Analog data, analog signals

- Modulation
  - Process of combining an input signal  $m(t)$  and a carrier at frequency  $f_c$  to produce signal  $s(t)$  with bandwidth centered on  $f_c$

- Reasons for modulation
  - \* Higher frequency may be needed for effective transmission
  - \* Modulation permits frequency division multiplexing

- Amplitude modulation

- Simplest form of modulation
- Signal is expressed as

$$s(t) = [1 + n_a x(t)] \cos 2\pi f_c t$$

where  $\cos 2\pi f_c t$  is carrier and  $x(t)$  is the input signal with both normalized to unity amplitude;  $n_a$  is modulation index given by the ratio of amplitude of input signal to carrier

- Input signal is:  $m(t) = n_a x(t)$
- The additive 1 is a DC component to prevent loss of information
- Scheme is also known as double sideband transmitted carrier
- Example: expression for  $s(t)$  if  $x(t)$  is AM signal  $\cos 2\pi f_m t$

$$\begin{aligned} s(t) &= [1 + n_a \cos 2\pi f_m t] \cos 2\pi f_c t \\ &= \cos 2\pi f_c t + \frac{n_a}{2} \cos 2\pi(f_c \pm f_m)t \end{aligned}$$

- Resulting signal has a component at original carrier frequency as well as a pair of components each spaced  $f_m$  Hz from the carrier
- Effectively, AM involves multiplication of original signal by carrier
  - \* Envelope of resulting signal is  $[1 + n_a x(t)]$
  - \* With  $n_a < 1$ , envelope is an exact reproduction of original signal
  - \* With  $n_a > 1$ , envelope crosses the time axis and information is lost
- Spectrum of an AM signal
  - \* Figure 5.16
  - \* Spectrum of AM signal is the original carrier plus spectrum of original signal translated to  $f_c$
  - \* Portion of spectrum for  $|f| > |f_c|$  is *upper sideband*
  - \* Portion of spectrum for  $|f| < |f_c|$  is *lower sideband*
  - \* Consider a voice signal between 30–3000 Hz with  $f_c$  being 60 kHz
  - \* Upper sideband is given by 60.3–63 kHz
  - \* Lower sideband is given by 57–59.7 kHz
  - \* Total transmitted power  $P_t$  in  $s(t)$  is given by

$$P_t = P_c \left( 1 + \frac{n_a^2}{2} \right)$$

where  $P_c$  is the transmitted power in carrier

- \*  $n_a$  should be maximized (but  $< 1$ ) to allow most of the signal power to carry information

- Angle modulation

- Encompasses frequency modulation (FM) and phase modulation (PM) as special cases
- Modulated signal is given by

$$s(t) = A_c \cos[2\pi f_c t + \phi(t)]$$

- Phase modulation

- \* Phase is proportional to modulating signal

$$\phi(t) = n_p m(t)$$

where  $n_p$  is phase modulation index

- Frequency modulation

- \* Derivative of phase is proportional to modulating signal

$$\phi'(t) = n_f m(t)$$

where  $n_f$  is frequency modulation index

## Spread spectrum

- Can be used to transmit either analog or digital data, using analog signal
- Spread the information signal over a wider bandwidth to make jamming and interception more difficult
- Figure 5.19
- Channel encoder
  - Receives input and converts it into an analog signal with relatively narrow bandwidth around some center frequency
  - Signal is further modulated using a pseudorandom sequence
    - \* Modulation spreads the spectrum (increases the bandwidth) of the signal to be transmitted
    - \* Pseudorandom numbers are dependent on seed and random number generator algorithm
- Channel decoder
  - Uses the same pseudorandom sequence to demodulate the spread spectrum signal
- Frequency hopping
  - Signal is broadcast over seemingly random sequence of radio frequencies, hopping from one to another in split-second interval
  - Receiver also hops on the same frequencies in synchronization with the sender
  - Difficult to catch the signal if you do not know the frequencies
  - Cannot jam the signal if you do not know the frequencies
- Direct sequence
  - Each bit in original code is represented by multiple bits in the transmitted signal
  - Multiple bits are known as *chipping code*
  - Chipping code spreads the signal across a wider frequency band in direct proportion to the number of bits used
    - \* A 10-bit chipping code spreads the signal across a frequency band that is 10 times greater than the 1-bit chipping code
  - Combine the digital information stream with the pseudorandom bit stream using an exclusive-or
  - Figure 5.21