

**Important:** This is an open book test. You can use any books, notes, or paper.

1. [6 pt] What is the maximum number of possible different shades of gray in an RGB image whose three component images are 8-bit images?
2. [10 pt] Show that the saturation component of the complement of a color image cannot be computed from the saturation component of the input image alone.
3. [10 pt] Consider an 8-pixel line of intensity data  $\{108, 139, 135, 244, 172, 173, 56, 99\}$ . If it is uniformly quantized with a 4-bit accuracy, compute the rms error and rms signal-to-noise ratios for the quantized data.
4. [10 pt] Consider the simple  $4 \times 8$ , 8-bit image:

|    |    |    |    |     |     |     |     |
|----|----|----|----|-----|-----|-----|-----|
| 21 | 21 | 21 | 95 | 169 | 243 | 243 | 243 |
| 21 | 21 | 21 | 95 | 169 | 243 | 243 | 243 |
| 21 | 21 | 21 | 95 | 169 | 243 | 243 | 243 |
| 21 | 21 | 21 | 95 | 169 | 243 | 243 | 243 |

- (a) Compute the entropy of the image.
  - (b) Compress the image using Huffman coding.
  - (c) Compute the compression achieved and the effectiveness of Huffman coding.
5. [14 pt] Compute Golomb code  $G_5(n)$  for  $0 \leq n \leq 7$ .
6. [8 pt] Given a four-symbol source  $[a, b, c, d]$  with source probabilities  $[0.1, 0.4, 0.3, 0.2]$ , arithmetically encode the sequence  $bbadc$ .
7. [10 pt] Erosion of a set  $A$  by structuring element  $B$  is a subset of  $A$ , provided that the origin of  $B$  lies within  $B$ . Give an example in which the erosion  $A \ominus B$  lies outside, or partially outside,  $A$ .