Important: This is an open book test. You can use any books, notes, or paper, but not exchange anything with other students. You are not allowed to use any electronic/communication devices, including a calculator and e-books. *Do not log into the computer during the test. Switch off your cell phones. Any device with an ON-OFF switch should have its switch in the OFF position*. Any calculations and rough work can be done on the back side of the test pages. You will lose five points for not writing your name.

1. [10 pt] A CCD camera chip of dimensions 4×4 mm and having 128×128 elements is focused on a square flat area 8m away. How many line pairs per mm will this camera be able to resolve? The camera is equipped with a 35mm lens.

2. [10 pt] Consider the two image subsets S_1 and S_2 , shown in the following figure. For $V = \{1\}$, determine whether these subsets are (a) 4-adjacent, (b) 8-adjacent, or (c) m-adjacent.

| | S_1 | | | | S_2 | | | | |
|---|-------|---|------------------|---|-------|---|---|---|---|
| 0 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 1 |
| 0 | 1 | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 1 |
| 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 1 0 0 | 1 | 0 | 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 1 |

3. [10 pt] Show that the median filter is a nonlinear filter.

4. [10 pt] With respect to the following figures, sketch the set $(A \cap B) \cup (A \cup B)^c$. Treat A^c as complement of A

| | | \boldsymbol{A} | | | | | B | | |
|------------------|---|------------------|---|---|---|---|---|---|---|
| 1 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| 1 1 0 0 | 1 | 0 | 1 | 0 | 1 | 1 | 0 | 1 | 0 |
| 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 1 | 0 | 0 | 1 | 0 | 1 |

5. [10 pt] The probability distribution of pixel intensities in a 3-bit image is given as 0.21, 0.08, 0.09, 0.07, 0.27, 0.19, 0.04, 0.05

Create a lookup table to equalize this histogram.

6. [10 pt] Propose a set of intensity-slicing transformations capable of producing all the individual bit planes of an 8-bit monochrome image. For example, a transformation function with the property

$$T(r) = \begin{cases} 0 & \text{if } r \in [0, 127] \\ 255 & \text{if } r \in [128, 255] \end{cases}$$

produces an image of the 8th bit plane in a 8-bit image. It will be nice to show a single function that will output the ith bit plane with the input being an unsigned char and i, with the output being the pixel value for ith bit plane.